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Dependency grammar and dependency parsing

Syntactic analysis (5LN455)

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Ali Basirat

Department of Linguistics and Philology

Based on slides from Marco Kuhlmann





Overview

- Arc-factored dependency parsing
 - Collins' algorithm
 - Eisner's algorithm
- Evaluation of dependency parsers
- Transition-based dependency parsing
 - The arc-standard algorithm
- Projectivity
- Advanced dependency parsing



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Dependency grammar



Dependency grammar

- The term ‘dependency grammar’ does not refer to a specific grammar formalism.
- Rather, it refers to a specific way to describe the syntactic structure of a sentence.

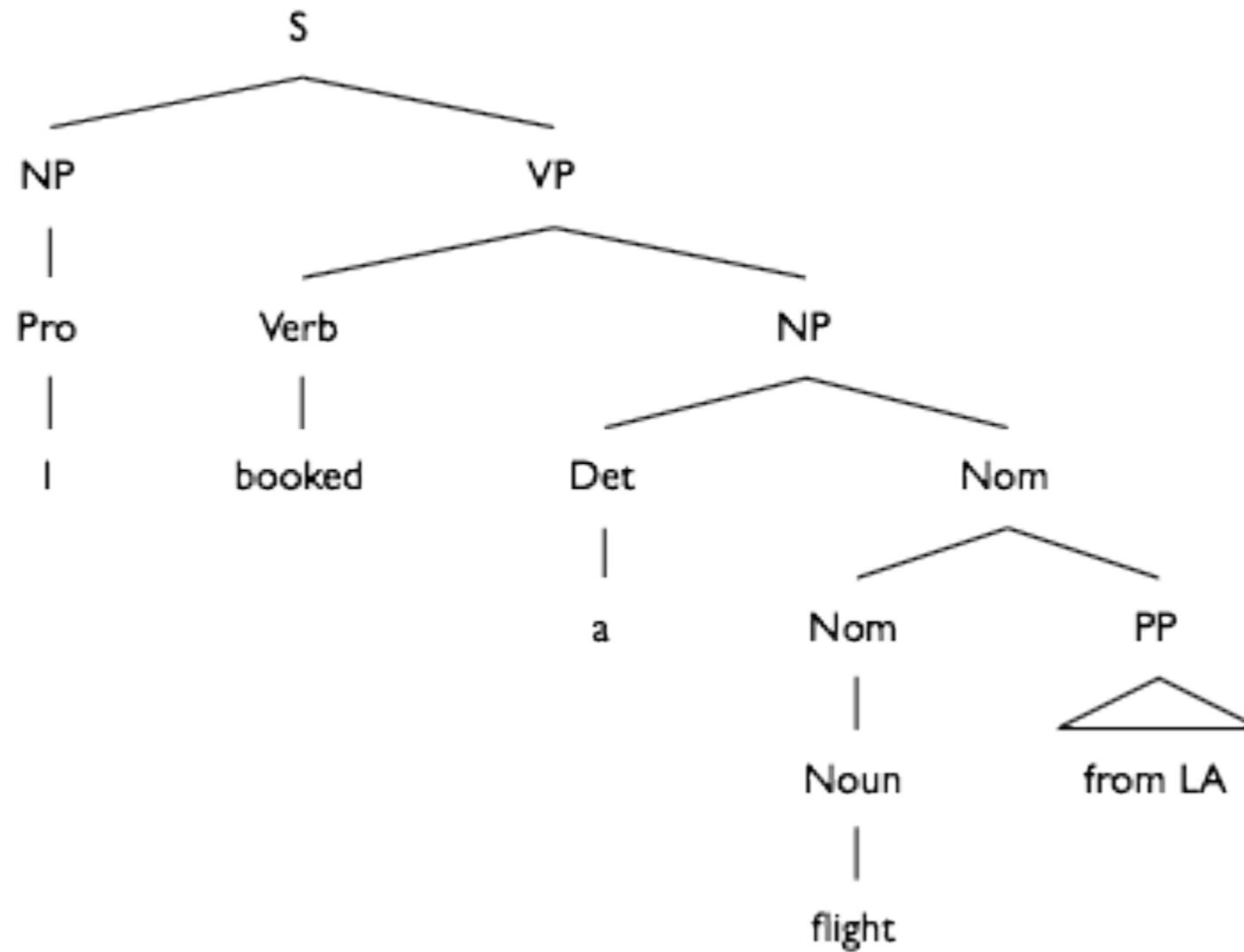


The notion of dependency

- The basic observation behind **constituency** is that groups of words may act as one unit.
 - *Example:* noun phrase, prepositional phrase
- The basic observation behind **dependency** is that words have grammatical functions with respect to other words in the sentence.
 - *Example:* subject, modifier

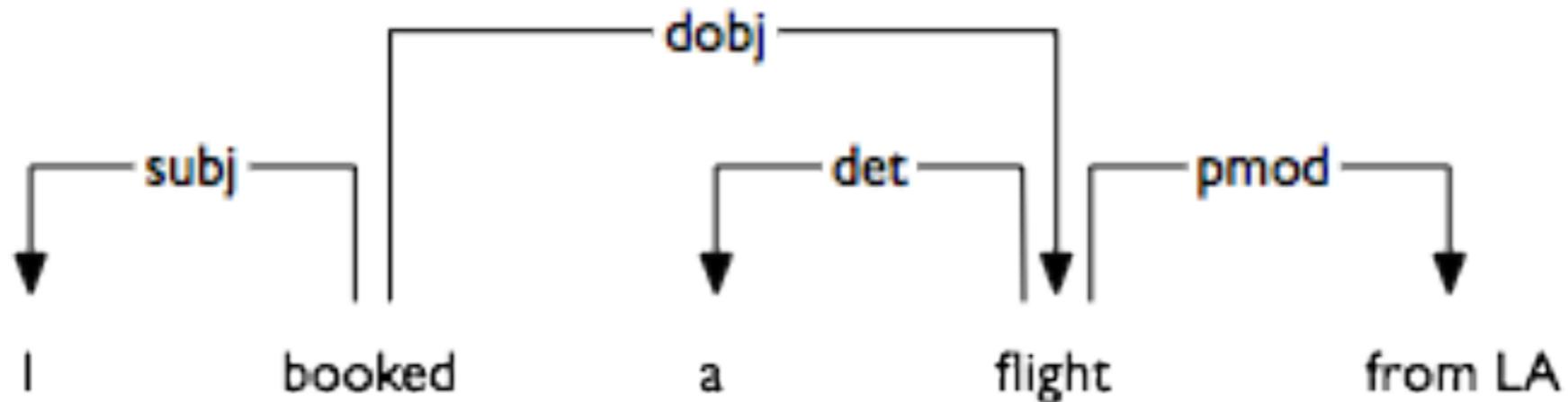


Phrase structure trees





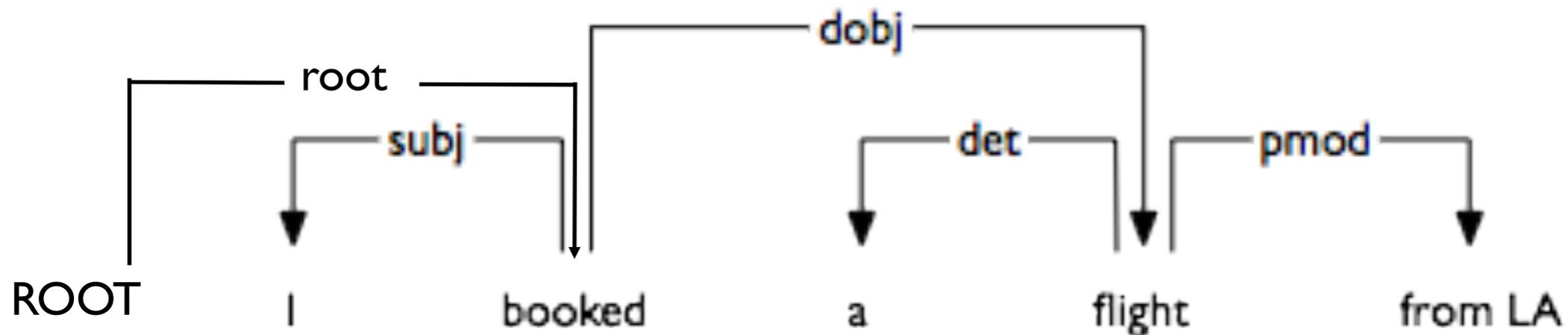
Dependency trees



- In an arc $h \rightarrow d$, the word h is called the **head**, and the word d is called the **dependent**.
- The arcs form a **rooted tree**.
- Each arc has a **label**, l , and an arc can be described as (h, d, l)



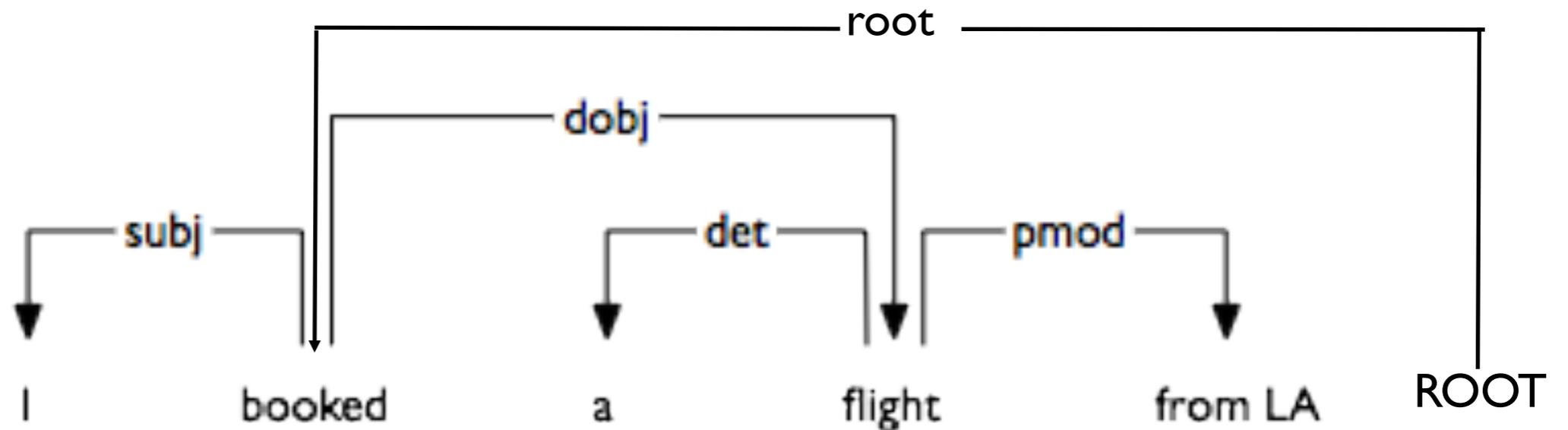
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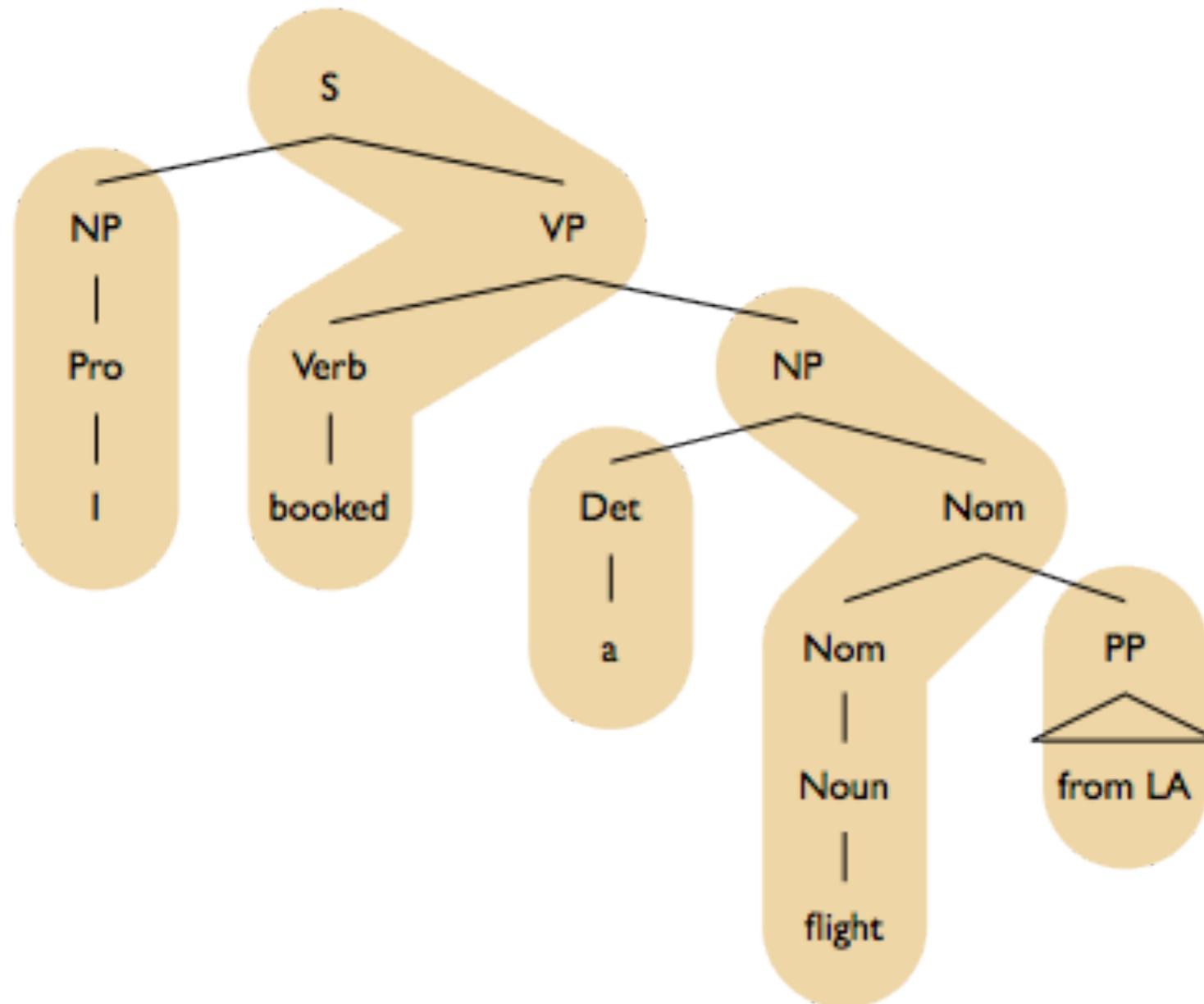


Heads in phrase structure grammar

- In phrase structure grammar, ideas from dependency grammar can be found in the notion of **heads**.
- Roughly speaking, the head of a phrase is the most important word of the phrase: the word that determines the phrase function.
- *Examples:* noun in a noun phrase, preposition in a prepositional phrase



Heads in phrase structure grammar





Linguistic resources

- Dependency treebanks exist for a wide range of natural languages.
- These treebanks can be used to train accurate and efficient dependency parsers.
- We will not use grammars in the parsing algorithms we discuss in the course

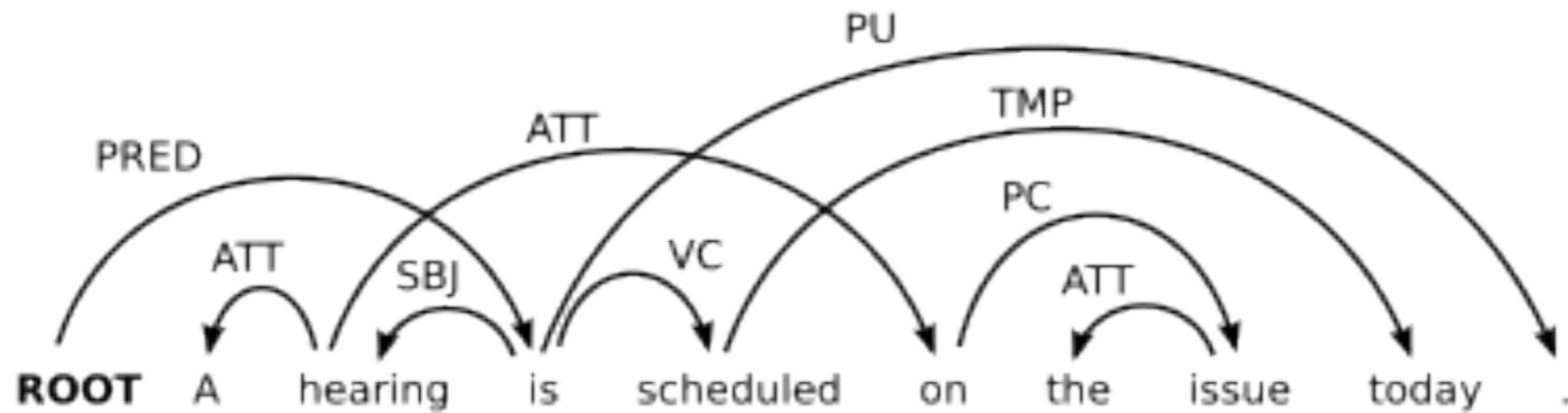
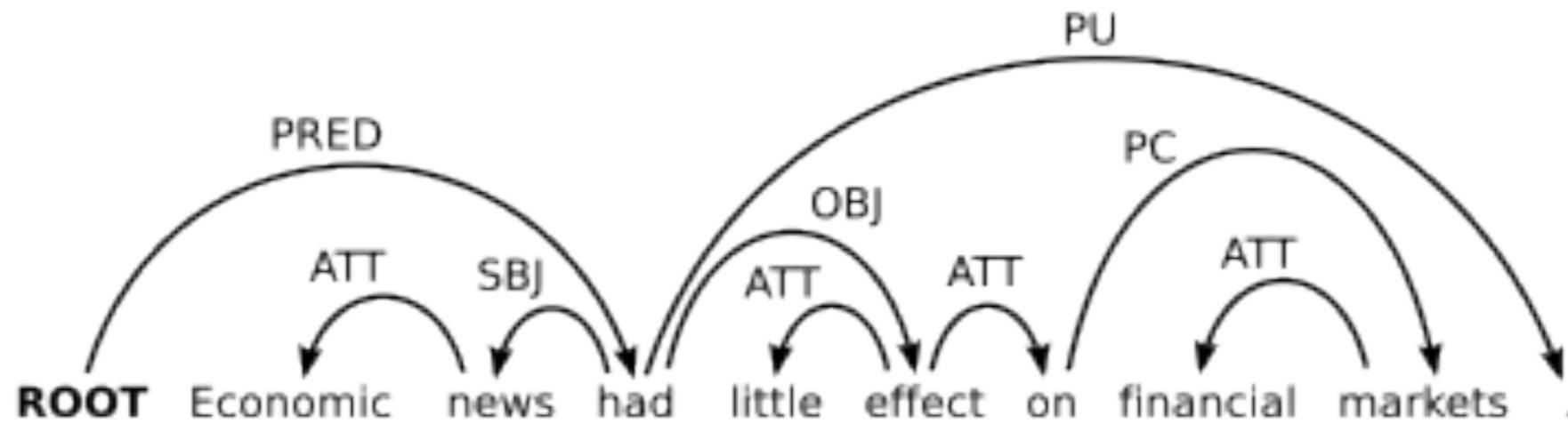


Projectivity

- An important characteristic of dependency trees is projectivity
- A dependency tree is projective if:
 - For every arc in the tree, there is a directed path from the head of the arc to all words occurring between the head and the dependent (that is, the arc (i,l,j) implies that $i \rightarrow^* k$ for every k such that $\min(i, j) < k < \max(i, j)$)



Projective and non-projective trees





Projectivity and dependency parsing

- Many dependency parsing algorithms can only handle projective trees
- Non-projective trees do occur in natural language
 - How often depends on the language (and treebank)



Projectivity in the course

- The algorithms we will discuss in detail during the lectures will only concern projective parsing
- Non-projective parsing:
 - You can read more about it in the course book!



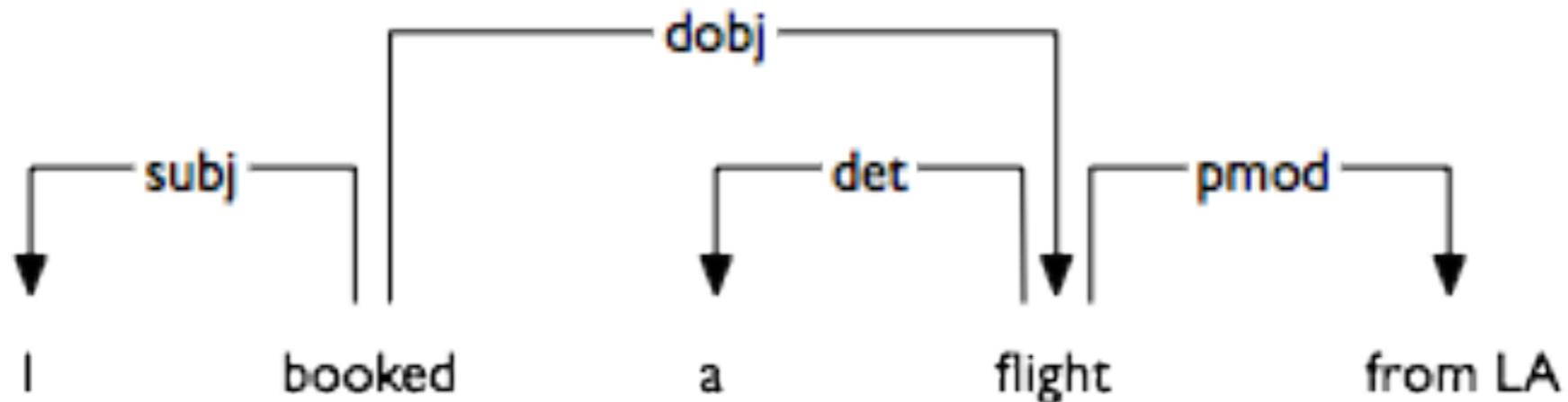
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Arc-factored dependency parsing



Ambiguity

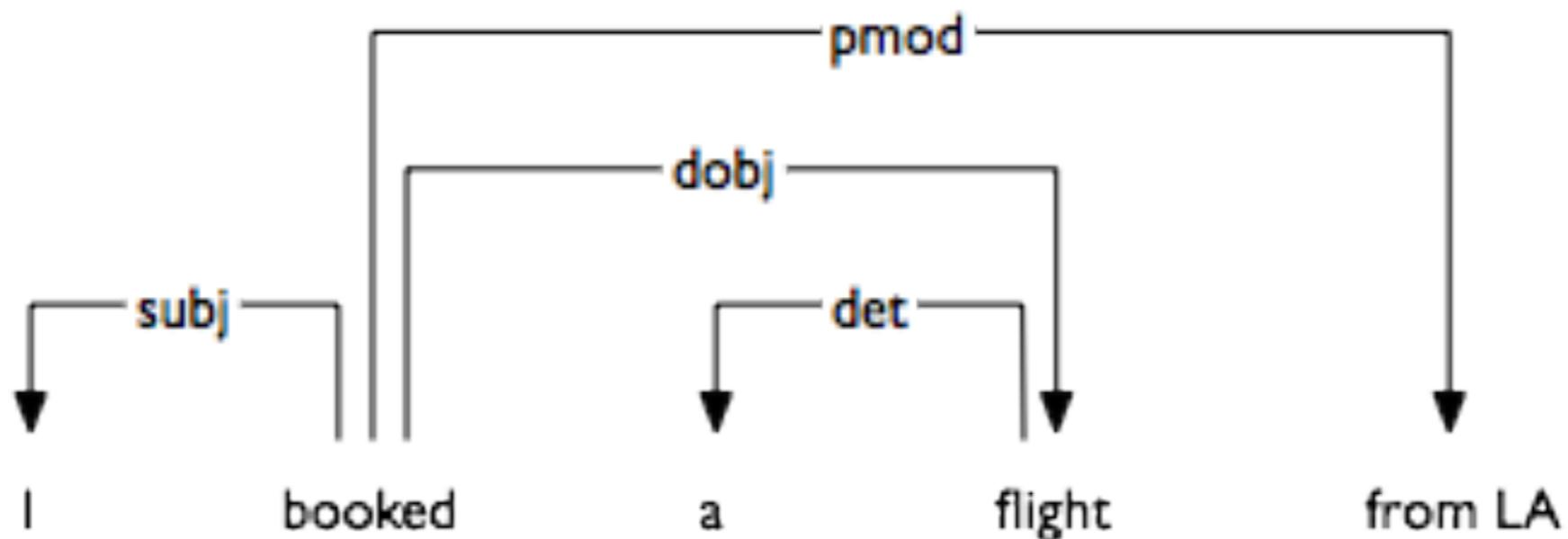
Just like phrase structure parsing,
dependency parsing has to deal with ambiguity.





Ambiguity

Just like phrase structure parsing,
dependency parsing has to deal with ambiguity.





Disambiguation

- We need to **disambiguate** between alternative analyses.
- We develop mechanisms for scoring dependency trees, and disambiguate by choosing a dependency tree with the highest score.



Scoring models and parsing algorithms

- Distinguish two aspects:

- **Scoring model:**

How do we want to score dependency trees?

- **Parsing algorithm:**

How do we compute a highest-scoring dependency tree under the given scoring model?



The arc-factored model

- Split the dependency tree t into **parts** p_1, \dots, p_n , score each of the parts individually, and combine the score into a simple sum.
- $\text{score}(t) = \text{score}(p_1) + \dots + \text{score}(p_n)$
- The simplest scoring model is the **arc-factored model**, where the scored parts are the arcs of the tree.



The arc-factored model

$$Score(x, y) = \sum_{(i,l,j) \in A_y} Score(i, l, j, x)$$

- A_y is the arc set of the dependency tree y
- $Score(i, l, j, x)$ is the score of the arc (i, l, j) for the sentence x



The arc-factored model

- The best parse tree is one with the highest score

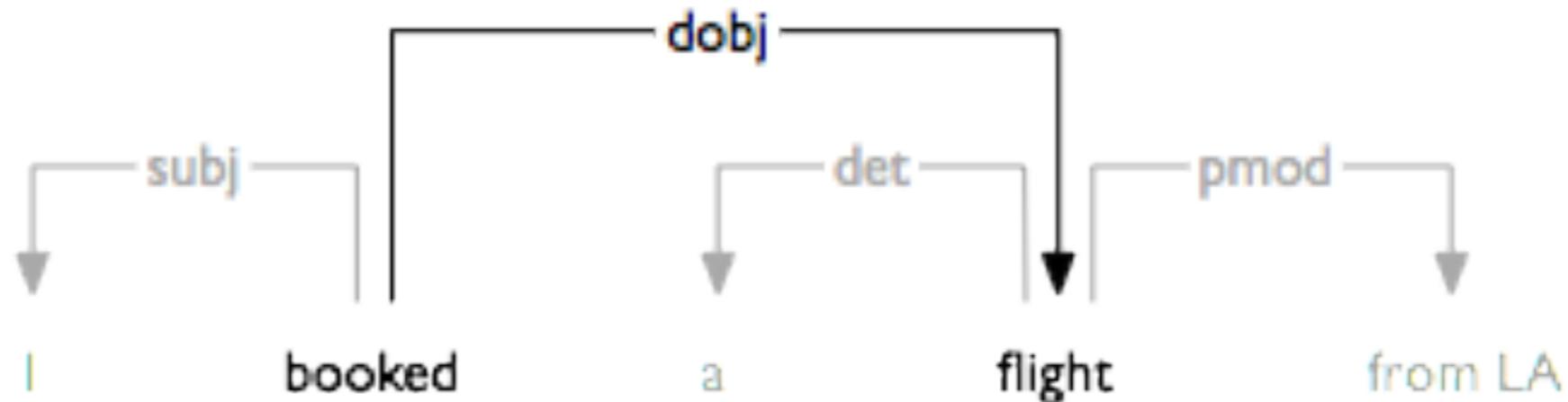
$$y^* = \underset{y \in GEN(x)}{argmax} \sum_{(i,l,j) \in A_y} Score(i, l, j, x)$$

- $GEN(x)$ is the set of all spanning trees

$$\begin{aligned} GEN(x) &= \{y \mid y \text{ is a spanning tree in } G_x \\ &= (V_x, V_x * l * V_x)\} \end{aligned}$$



Features



- To score an arc, we define **features** that are likely to be relevant in the context of parsing.
- We represent an arc by its **feature vector**.



Examples of features

- ‘The head is a verb.’
- ‘The dependent is a noun.’
- ‘The head is a verb
and the dependent is a noun.’
- ‘The head is a verb
and the predecessor of the head is a pronoun.’
- ‘The arc goes from left to right.’
- ‘The arc has length 2.’



Feature vectors





Implementation of feature vectors

- We assign each feature a unique number.
- For each arc, we collect the numbers of those features that apply to that arc.
- The feature vector of the arc is the list of those numbers.
- *Example:* [1, 2, 42, 313, 1977, 2008, 2010]



Feature weights

- Arc-factored dependency parsers require a training phase.
- During training, our goal is to assign, to each feature f_i , a **feature weight** w_i .
- Intuitively, the weight w_i quantifies the effect of the feature f_i on the likelihood of the arc.
- *How likely is it that we will see an arc with this feature in a useful dependency tree?*



Feature weights

- We define the **score** of an arc $h \rightarrow d$ as the weighted sum of all features of that arc:
- $\text{score}(h \rightarrow d) = f_1 w_1 + \dots + f_n w_n$



Feature weights

$$\text{score}(i, l, j, x) = \sum_{k=1}^n f_k(i, l, j, x) \cdot \mathbf{w}_k$$

- $f_k(i, l, j, x)$ is a feature function representing some salient property of the arc (i, l, j) in the context of x
- \mathbf{w}_k is a real-valued feature weight, reflecting the tendency of $f_k(i, l, j, x)$ to co-occur with a good or bad parse tree



Training using structured prediction

- Take a sentence w and a gold-standard dependency tree g for w .
- Compute the highest-scoring dependency tree under the current weights; call it p .
- Increase the weights of all features that are in g but not in p .
- Decrease the weights of all features that are in p but not in g .



Training using structured prediction

Training data: $\mathcal{T} = \{(x^i, y^i)\}_{i=1}^{|\mathcal{T}|}$

```
1  $\mathbf{w} \leftarrow 0$ 
2 for  $n : 1..N$ 
3   for  $i : 1..|\mathcal{T}|$ 
4      $y^* \leftarrow \text{PARSE}(x^i, \mathbf{w})$ 
5     if  $y^* \neq y^i$ 
6        $\mathbf{w} \leftarrow \text{UPDATE}(\mathbf{w}, y^*, y^i)$ 
7 return  $\mathbf{w}$ 
```

$\text{PARSE}(x, \mathbf{w})$

```
1 return  $\text{argmax}_{y \in \text{GEN}(x^i)} \sum_{(i,l,j) \in A_y} \sum_{k=1}^K \mathbf{f}_k(i, l, j, x^i) \cdot \mathbf{w}_k$ 
```

$\text{UPDATE}(\mathbf{w}, y^*, y^i)$

```
1 for  $k : 1..K$ 
2   for  $(i, l, j) \in A_{y^*}$ 
3      $\mathbf{w}_k \leftarrow \mathbf{w}_k - \mathbf{f}_k(i, l, j, x)$ 
4   for  $(i, l, j) \in A_{y^i}$ 
5      $\mathbf{w}_k \leftarrow \mathbf{w}_k + \mathbf{f}_k(i, l, j, x)$ 
```



Training using structured prediction

- Training involves repeatedly parsing (treebank) sentences and refining the weights.
- Hence, training presupposes an efficient parsing algorithm.



Parsing algorithms

- Projective parsing
 - Inspired by the CKY algorithm
 - Collins' algorithm
 - Eisner's algorithm
- Non-projective parsing:
 - Minimum spanning tree (MST) algorithms



Graph-based parsing

- Arc-factored parsing is an instance of graph-based dependency parsing
- Because it scores the dependency graph (tree)
- Graph-based models are often contrasted with transition-based models
- There are also grammar-based methods, which we will not discuss



Summary

- The term ‘arc-factored dependency parsing’ refers to dependency parsers that score a dependency tree by scoring its arcs.
- Arcs are scored by defining features and assigning weights to these features.
- The resulting parsers can be trained using structured prediction.
- More powerful scoring models exist.



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Collins' algorithm



Collins' algorithm

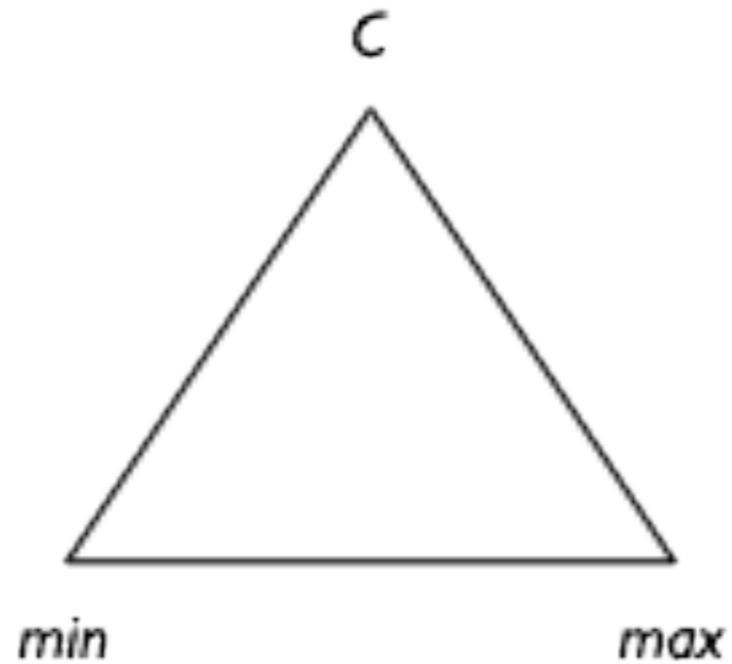
- Collins' algorithm is a simple algorithm for computing the highest-scoring dependency tree under an arc-factored scoring model.
- It can be understood as an extension of the CKY algorithm to dependency parsing.
- Like the CKY algorithm, it can be characterized as a bottom-up algorithm based on dynamic programming.



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Collins' algorithm

Signatures, CKY



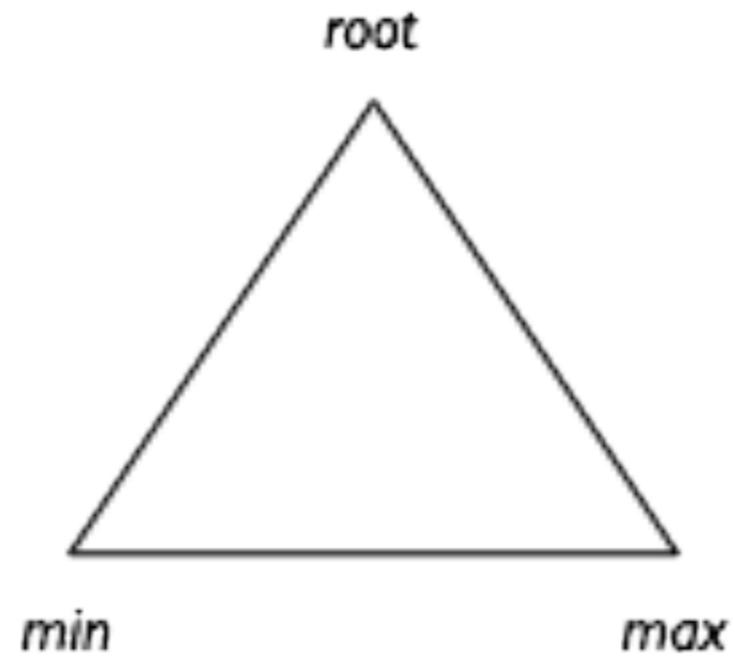
$[min, max, c]$



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Collins' algorithm

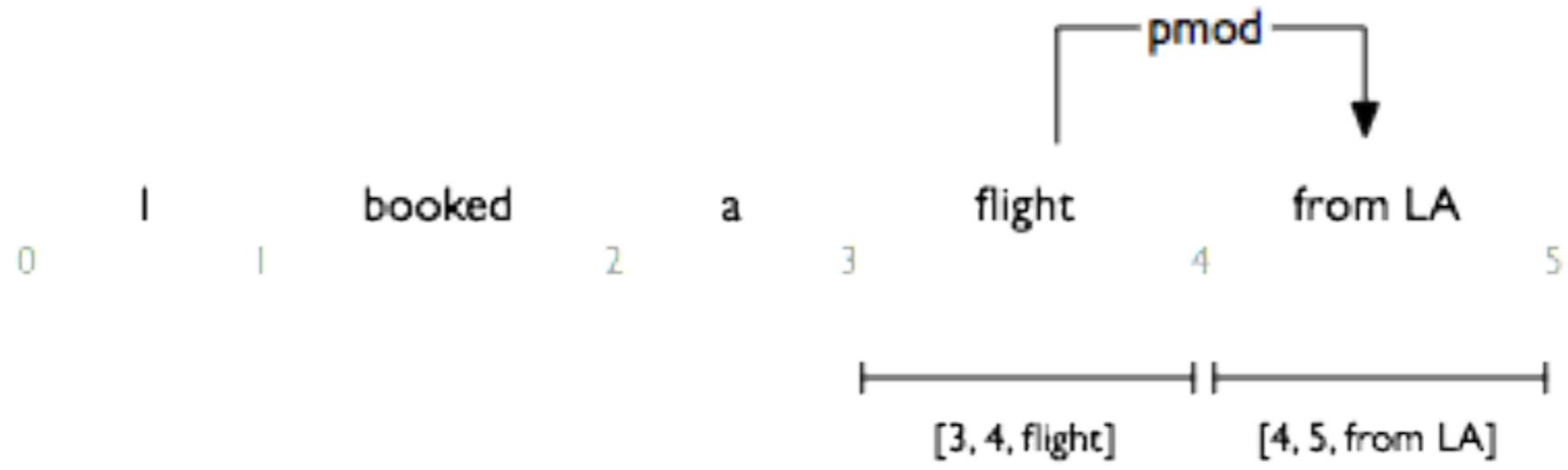
Signatures, Collins'



$[min, max, root]$

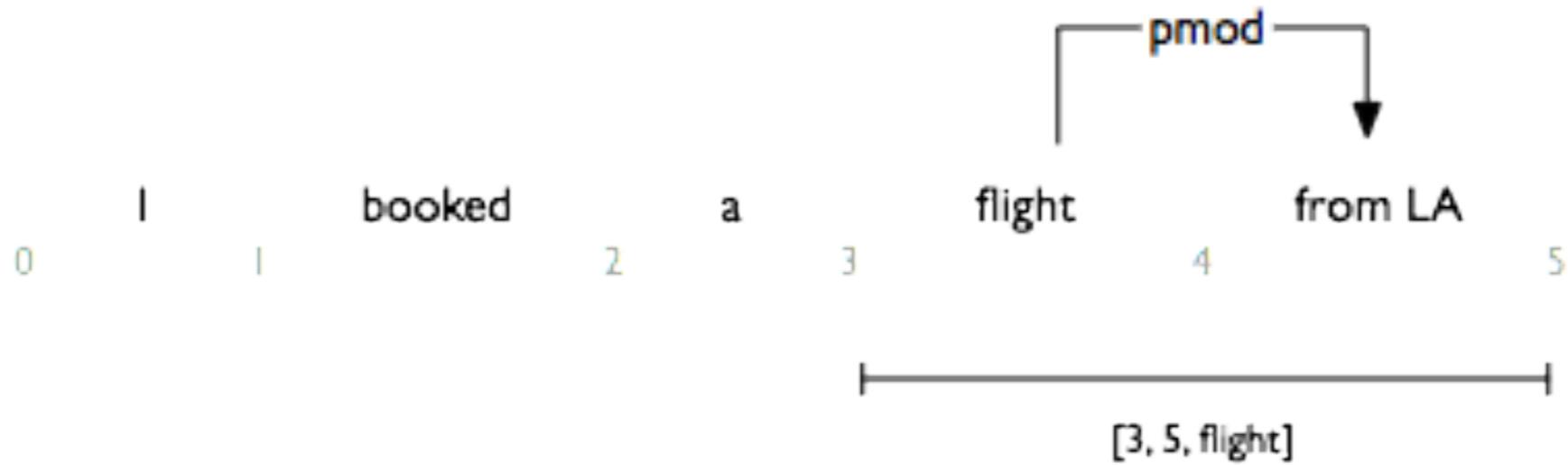


Adding a left-to-right arc





Adding a left-to-right arc

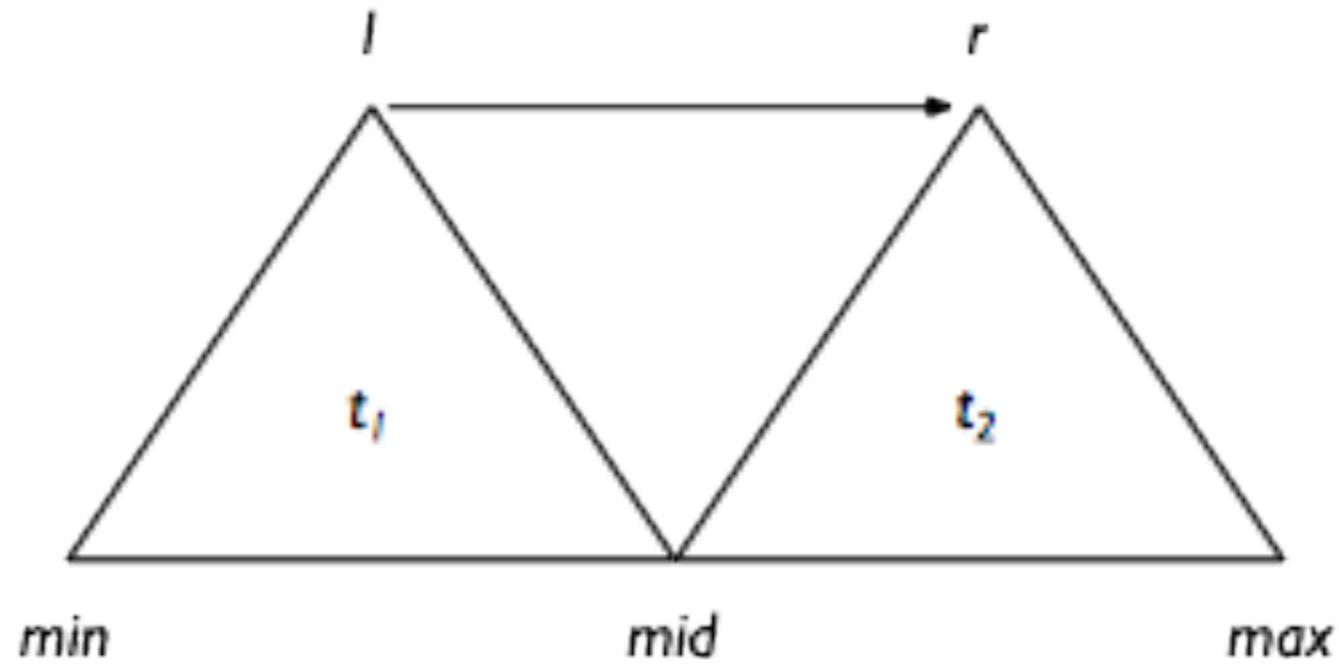




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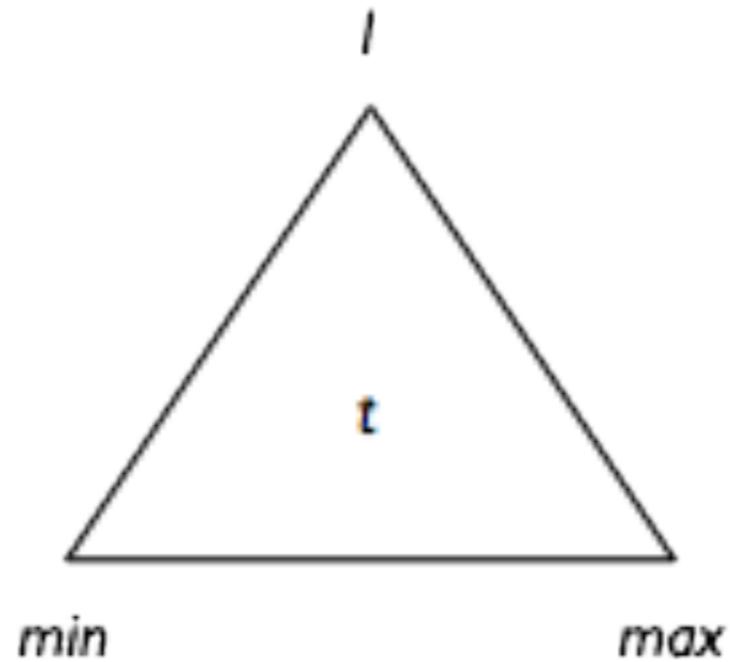
Collins' algorithm

Adding a left-to-right arc





Adding a left-to-right arc



$$\text{score}(t) = \text{score}(t_1) + \text{score}(t_2) + \text{score}(l \rightarrow r)$$

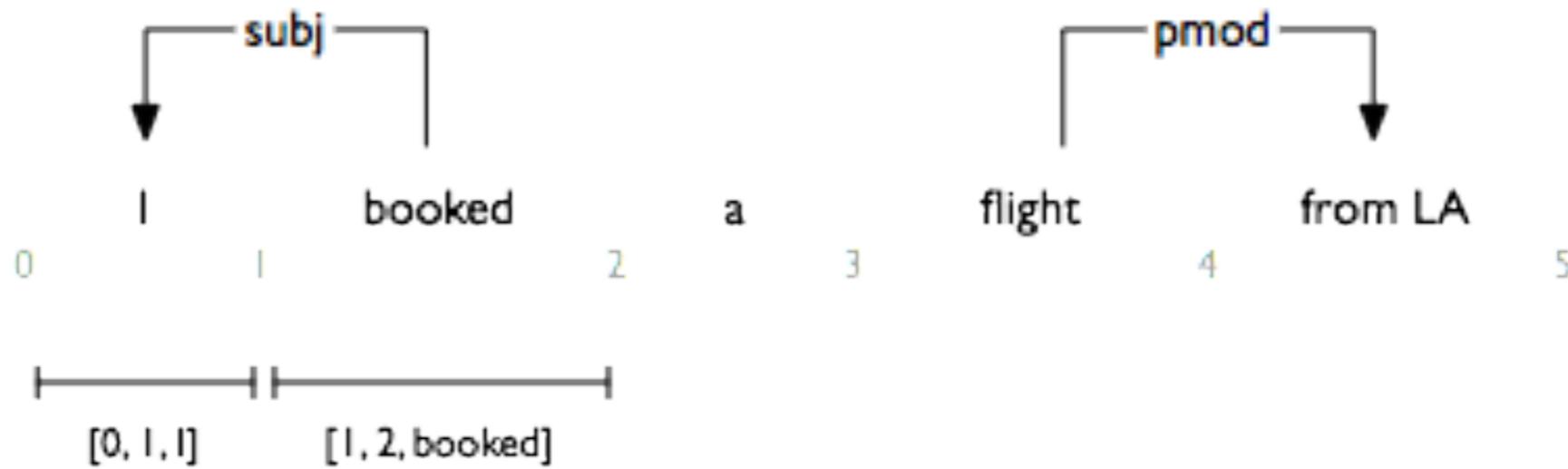


Adding a left-to-right arc

```
for each [min, max] with max - min > 1 do
  for each l from min to max - 2 do
    double best = score[min][max][l]
    for each r from l + 1 to max - 1 do
      for each mid from l + 1 to r do
        t1 = score[min][mid][l]
        t2 = score[mid][max][r]
        double current = t1 + t2 + score(l → r)
        if current > best then
          best = current
    score[min][max][l] = best
```



Adding a right-to-left arc





Adding a right-to-left arc

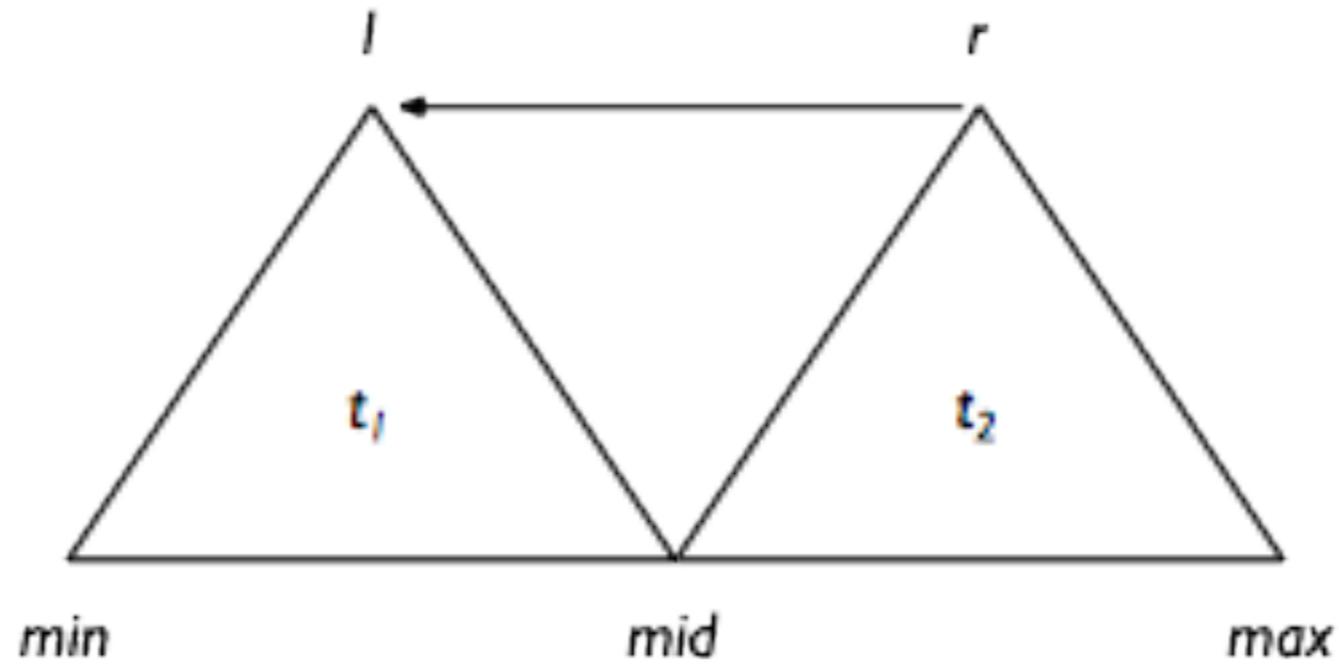




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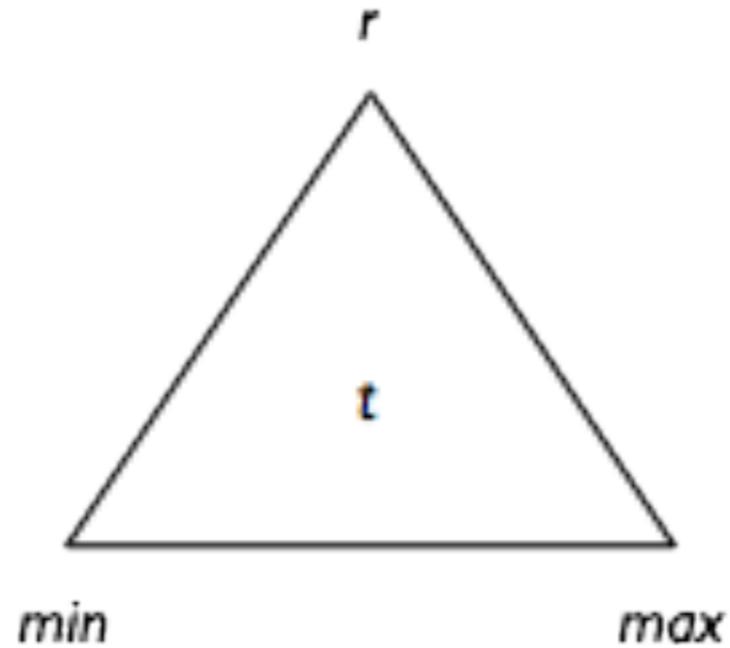
Collins' algorithm

Adding a right-to-left arc





Adding a right-to-left arc



$$\text{score}(t) = \text{score}(t_1) + \text{score}(t_2) + \text{score}(r \rightarrow l)$$

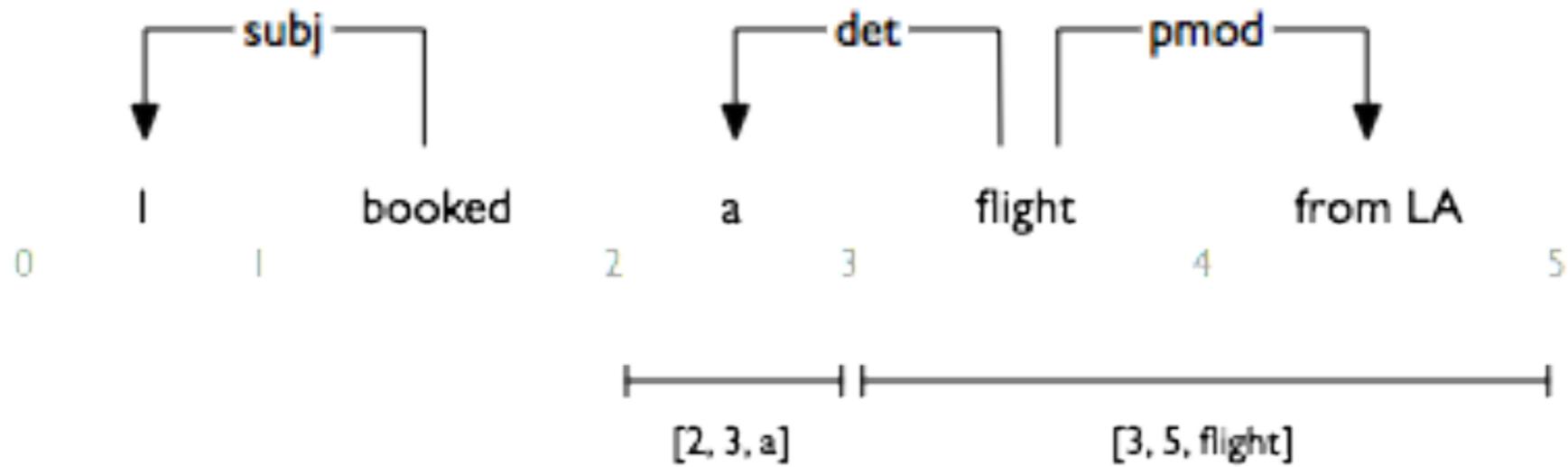


Adding a right-to-left arc

```
for each [min, max] with max - min > 1 do
  for each r from min + 1 to max - 1 do
    double best = score[min][max][r]
    for each l from min to r - 1 do
      for each mid from l + 1 to r do
        t1 = score[min][mid][l]
        t2 = score[mid][max][r]
        double current = t1 + t2 + score(r → l)
        if current > best then
          best = current
    score[min][max][r] = best
```

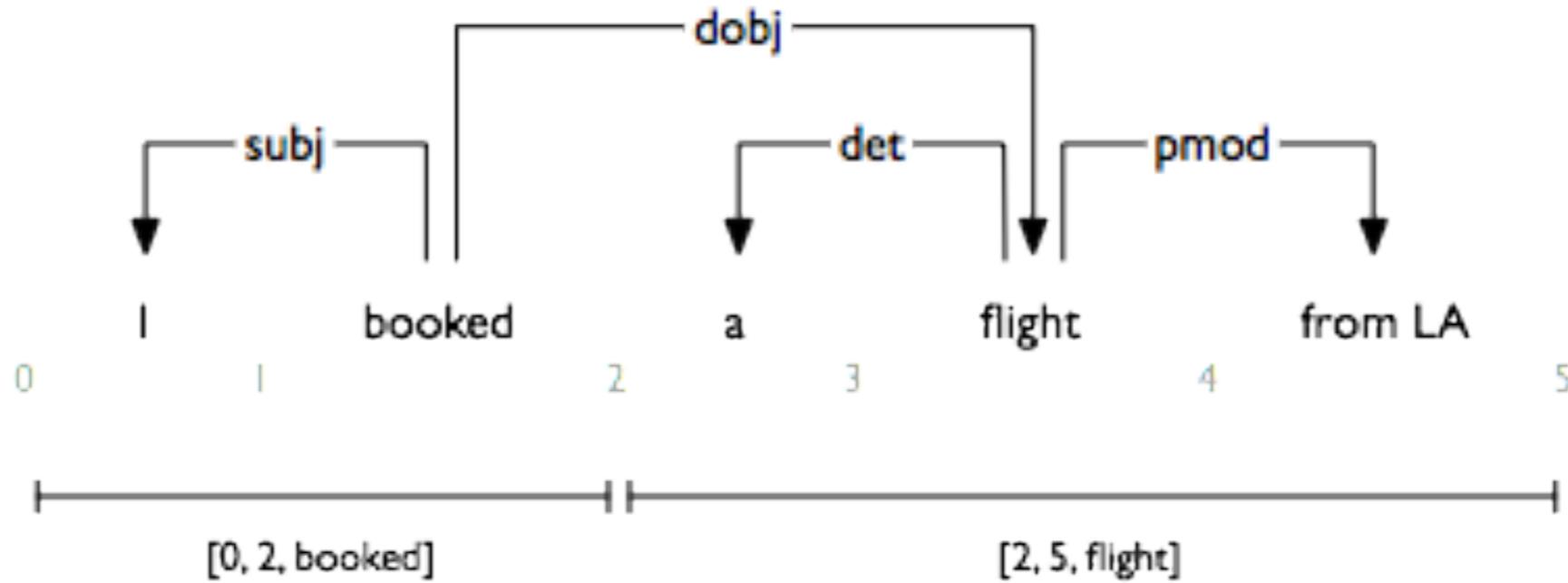


Finishing up



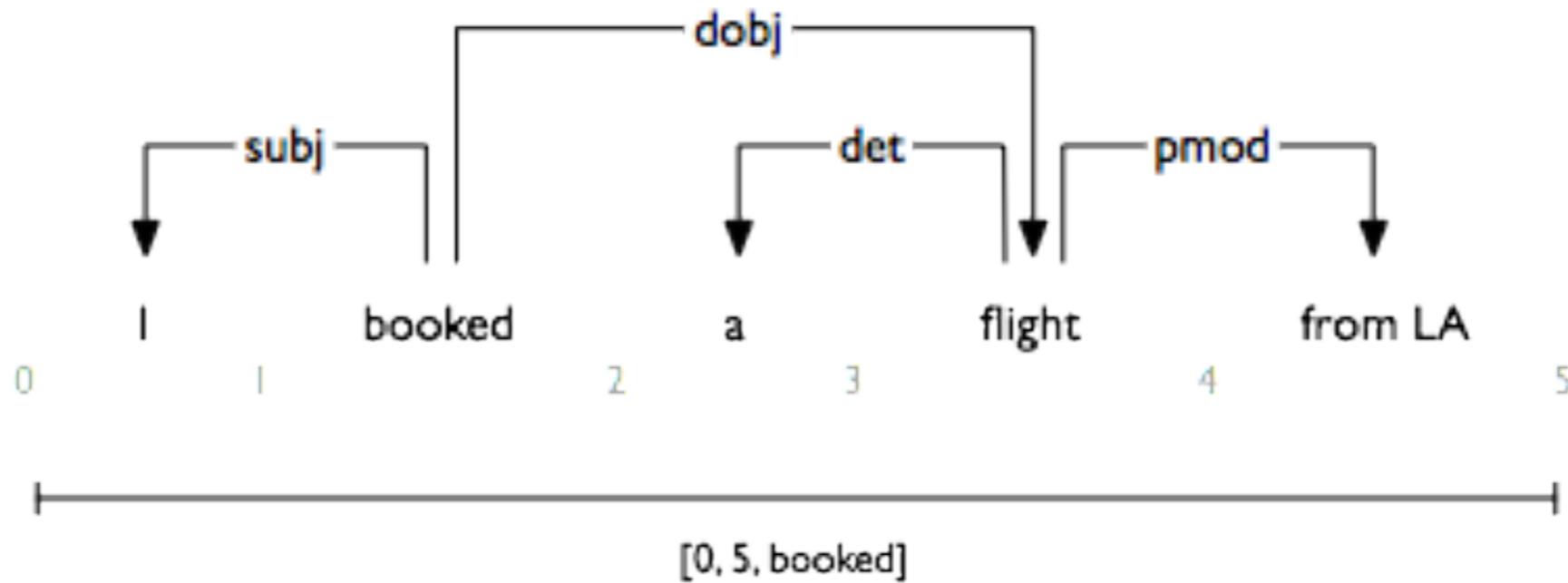


Finishing up





Finishing up





Complexity analysis

- Runtime?
- Space?

```
for each [min, max] with max - min > 1 do
```

```
  for each r from min + 1 to max - 1 do
```

```
    double best = score[min][max][r]
```

```
    for each l from min to r - 1 do
```

```
      for each mid from l + 1 to r do
```

```
        t1 = score[min][mid][l]
```

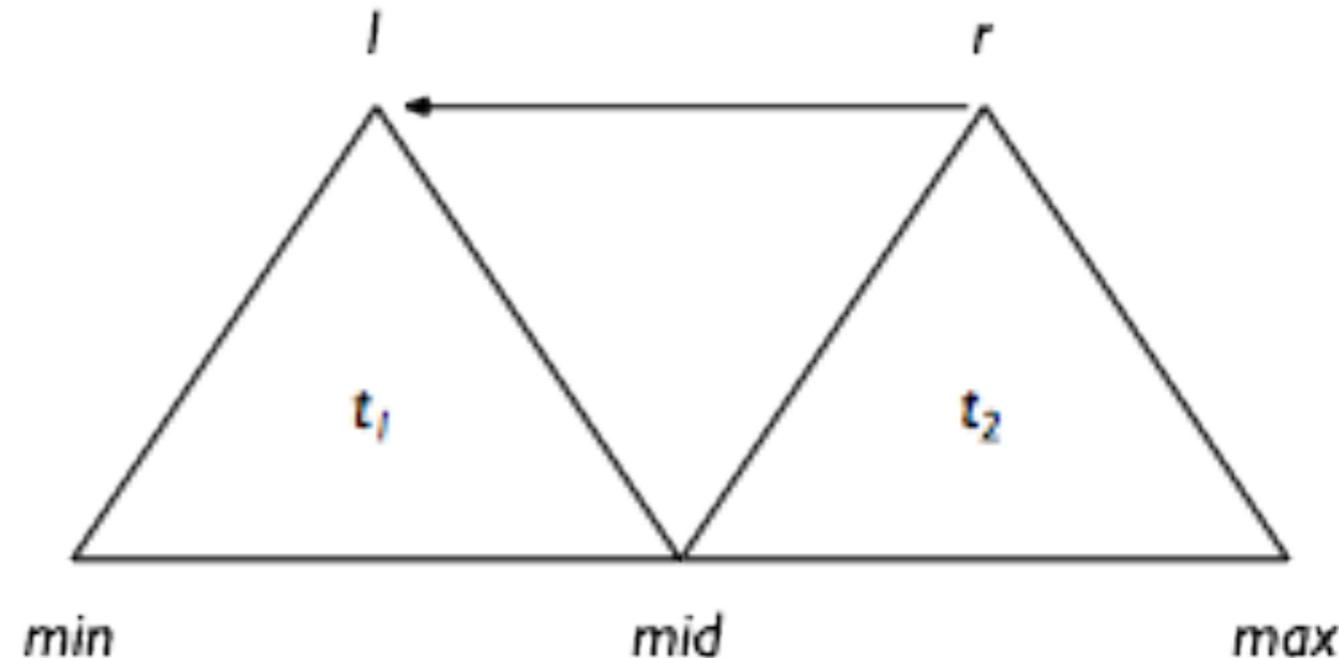
```
        t2 = score[mid][max][r]
```

```
        double current = t1 + t2 + score(r → l)
```

```
        if current > best then
```

```
          best = current
```

```
      score[min][max][r] = best
```





Complexity analysis

- Space requirement:
 $O(|w|^3)$
- Runtime requirement:
 $O(|w|^5)$



Summary

- Collins' algorithm is a CKY-style algorithm for computing the highest-scoring dependency tree under an arc-factored scoring model.
- It runs in time $O(|w|^5)$.
This may not be practical for long sentences.
- We have not discussed labels yet - we will do that in the next lecture